

Q. No. 2 Part (i) (Page 1)

$$2y^3 - 3xy^2 + 2x^2y + 5x = 6$$

Differentiate wrt x

$$6y^2 \frac{dy}{dx} - 3\left(x \cdot 2y \frac{dy}{dx} + y^2(1)\right) - 2\left(x^2 \frac{dy}{dx} + 2xy\right) + 5 = 0$$

$$6y^2 \frac{dy}{dx} - 6x \frac{dy}{dx} - 3y^2 - 2x^2 \frac{dy}{dx} - 4xy + 5 = 0$$

$$\frac{dy}{dx} (6y^2 - 6x - 2x^2) = 3y^2 + 4xy - 5$$

$$\frac{dy}{dx} = \frac{3y^2 + 4xy - 5}{6y^2 - 6x - 2x^2}$$

$$\begin{aligned} \frac{dy}{dx} \Big|_{(1,1)} &= \frac{3(1)^2 + 4(1)(1) - 5}{6(1)^2 - 6(1) - 2(1)^2} \\ &= \frac{3 + 4 - 5}{6 - 6 - 2} \\ &= \frac{2}{-2} \end{aligned}$$

$$\frac{dy}{dx} \Big|_{(1,1)} = -1$$

Q. No. 2 Part (ii) (Page 1)

$$f(x) = \begin{cases} 3x-1 & \text{if } x < 1 \\ 4 & \text{if } x = 1 \\ 2x & \text{if } x > 1 \end{cases}$$

Discuss continuity at $x=1$

$$f(x) = 4$$

$$f(1) = 4$$

$$\text{LHL} = \lim_{x \rightarrow 1^-} 3x-1 = 3(1)-1$$

$$= 2$$

$$\text{RHL} = \lim_{x \rightarrow 1^+} 2x = 2(1)$$

$$= 2$$

$$\text{LHL} = \text{RHL} \neq f(x)$$

Hence it is not continuous.

Q. No. 2 Part (iii) (Page 1)

Evaluate $\lim_{\theta \rightarrow 0} \frac{\sec \theta - 1}{\theta \sec \theta} \left(\frac{0}{0} \right) \frac{1}{\cos \theta} - 1$

or differentiate

$$\lim_{\theta \rightarrow 0} \frac{1 - \cos \theta}{\theta \cdot \frac{1}{\cos \theta}} = \frac{(1 - \cos \theta) / \cos \theta}{\theta / \cos \theta}$$

$\frac{d(1 - \cos \theta)}{d\theta} = \sin \theta$ $\frac{d(\theta / \cos \theta)}{d\theta} = \frac{\cos \theta - \theta \sin \theta}{\cos^2 \theta}$

$$\lim_{\theta \rightarrow 0} \frac{\sin \theta}{\cos \theta - \theta \sin \theta} = \frac{2 \sin^2 \theta / 2}{\theta}$$

$$= \lim_{\theta \rightarrow 0} \frac{\sin^2 \theta / 2}{\theta / 2} = \lim_{\theta \rightarrow 0} \sin \theta / 2$$

$$= 1 \cdot 0$$

$$= 0$$

Q. No. 2 Part (iv) (Page 1) $x = 60^\circ$ $dx = \delta x = 1^\circ$

$$f(x) \sin 60^\circ = y$$

$$f'(x) = \cos 60^\circ$$

$$dx = 1^\circ$$

$$dy = f'(x)dx$$

$$\sin(x + \delta x) = y + dy$$

$$= \sin 60^\circ + \cos 60^\circ (1^\circ)$$

$$= \frac{\sqrt{3}}{2} + \frac{1}{2} (0.01745)$$

$$(\sin 61^\circ) = 0.874$$

Q. No. 2 Part (v) (Page 1)

$$y = x^3 - 9x$$

$$x^3 - 9x = 0$$

$$x(x^2 - 9) = 0$$

$$x = 0 \quad x = \pm 3$$

$$(-3, 0) \quad , \quad (3, 3)$$

$$y = x^3 - 9x \quad -3 < x < 0 \quad +ve$$

$$y = x^3 - 9x \quad 0 < x < 3 \quad -ve$$

$$\text{Area} = \int_{-3}^0 (x^3 - 9x) dx + \int_0^3 -(x^3 - 9x) dx$$

$$= \left[\frac{x^4}{4} - \frac{9x^2}{2} \right]_{-3}^0 - \left[\frac{x^4}{4} - \frac{9x^2}{4} \right]_0^3$$

$$= \left(0 - \left(-\frac{81}{4} \right) \right) - \left(-\frac{81}{4} - 0 \right)$$

$$= \frac{81}{4} + \frac{81}{4}$$

$$\boxed{\text{Area} = \frac{81}{2}}$$

Q. No. 2 Part (vi) (Page 1)

$$\frac{dy}{dx} = \frac{3}{4} x^3 + x - 3$$

$$1 dy = \left(\frac{3}{4} x^3 + x - 3 \right) dx$$

$$y = \frac{3x^4}{4 \cdot 4} + \frac{x^2}{2} - 3x + C$$

$$y = \frac{3x^4}{16} + \frac{x^2}{2} - 3x + C$$

At $(y=0)$ $(x=2)$ ~~At~~

$$0 = \frac{3(2)^4}{16} + \frac{4}{2} - 3(2) + C$$

$$0 = 3 + 2 - 6$$

$$0 = -1 + C$$

$$\boxed{C = 1}$$

$$\boxed{y = \frac{3x^4}{16} + \frac{x^2}{2} - 3x + 1}$$

req equation

Q. No. 2 Part (vii) (Page 1)

$$\frac{-1}{2} \int \frac{x \sin^{-1} x (-2) dx}{\sqrt{1-x^2}}$$

$$= \frac{-1}{2} \int \frac{-2x(1-x^2)^{-1/2} \sin^{-1} x}{I} dx$$

$$= \frac{-1}{2} \left[\sin^{-1} x \int -2x(1-x^2)^{-1/2} dx - \int \frac{1}{\sqrt{1-x^2}} \int -2x(1-x^2)^{-1/2} dx \right]$$

$$= \frac{-1}{2} \left[\sin^{-1} x \frac{(1-x^2)^{1/2}}{1/2} - \int \frac{2(1-x^2)^{1/2}}{\sqrt{1-x^2}} dx + C \right]$$

$$= \frac{-1}{2} \left[2 \sin^{-1} x \sqrt{(1-x^2)} - 2 \int 1 dx + C \right]$$

$$= -\sin^{-1} x \sqrt{(1-x^2)} + x + C$$

Q. No. 2 Part (viii) (Page 1)

$$3x + 2y \geq 6$$

$$x + y \leq 4$$

$$x \geq 0, y \geq 0$$

corresponding eq

$$3x + 2y = 6$$

x	0	2
y	3	0
	A	B

$$x + y = 4$$

x	0	4
y	4	0
	C	D

Test points

$$0 \geq 6 \text{ (F)}$$

$$0 \leq 4 \text{ (T)}$$

on graph (2)

corner points

$$A (0, 3)$$

$$B (2, 0)$$

$$C (0, 4)$$

$$D (4, 0)$$

Q. No. 2 Part (ix) (Page 1)

equation of Parabola \rightarrow let $P(x, y)$ be a point on parabola
 $F(-3, 4)$
directrix $3x + 2y - 3 = 0$

$$|PF| = |PM|$$

$$\sqrt{(x+3)^2 + (y-4)^2} = \frac{|3x + 2y - 3|}{\sqrt{9 + 4}}$$

$$\left(\sqrt{13} \sqrt{x^2 + 6x + 9 + y^2 - 8y + 16} \right)^2 = (3x + 2y - 3)^2$$

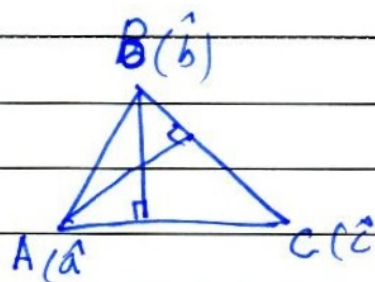
$$13(x^2 + 6x + 25 + y^2 - 8y) = 9x^2 + 4y^2 + 9 + 2(3x)(2y)$$

$$13x^2 + 78x + 325 + 13y^2 - 104y = 9x^2 + 4y^2 + 9 + 12xy + 2(2y)(-3) + 2(-3)(3x)$$

$$\boxed{4x^2 + 9y^2 + 96x - 92y + 316 - 12xy = 0}$$

Q. No. 2 Part (x) (Page 1)

A



Q. No. 2 Part (xi) (Page 1)

$$\frac{x^2}{18} + \frac{y^2}{8} = 1$$

$$8x^2 + 18y^2 = 144$$

$$\frac{x^2}{3} - \frac{y^2}{3} = 1$$

$$x^2 - y^2 = 3$$

$$x^2 = 3 + y^2$$

$$8(3 + y^2) + 18y^2 = 144$$

$$24 + 8y^2 + 18y^2 = 144$$

$$152y^2 = 120$$

$$y^2 = \frac{15}{19}$$

$$y = \pm \sqrt{\frac{15}{19}}$$

$$x^2 = 3 + y^2$$

$$= 3 + \frac{15}{19}$$

$$x^2 = \frac{72}{19}$$

$$x = \pm \sqrt{\frac{72}{19}}$$

intersection conics

$$\left(\pm \sqrt{\frac{72}{19}}, \pm \sqrt{\frac{15}{19}} \right)$$

Q. No. 2 Part (xii) (Page 1)

$$B = (1, 1, 1)$$

$$P = (2, 0, 1)$$

$$\text{Net Force} = 3i + 5j + k$$

~~PP~~

$$BP = OP - OB$$

$$= (2, 0, 1) - (1, 1, 1)$$

$$r = (1, -1, 0)$$

$$\tau = r \times F = \begin{vmatrix} i & j & k \\ 1 & -1 & 0 \\ 3 & 5 & 1 \end{vmatrix}$$

$$= i(-1+0) - j(1-0) + k(5+3)$$
$$\tau = -i - j + 8k$$

Q. No. 3 (Page 1)

Let x be the base of box and y be height and volume of open box be $V = 32 \text{ dm}^3$

$$V = x \cdot x \cdot h = x^2 h = x^2 y$$

$$32 = x^2 y$$

$$y = \frac{32}{x^2}$$

$$f(x) = \text{Volume of open box} = \text{area of base} + 4(\text{Surface area of sides}) \\ = x^2 + \frac{32}{x^2} = x^2 + 32x^{-2}$$

$$f(x) = x^2 + 32x^{-2}$$

$$f'(x) = 2x + -$$

$$f(x) = \begin{cases} px+2 & 0 \leq x < 2 \\ 7-qx & 2 \leq x < 4 \\ 2x+1 & 4 \leq x < 6 \end{cases}$$

* As $f(x)$ is continuous at $x=2$

$$f(x) = \text{LHL} = \text{RHL}$$

$$7-qx = \lim_{x \rightarrow 2^-} px+2 = \lim_{x \rightarrow 2^+} 7-qx$$

$$7-2q = 2p+2 = 7-2q \rightarrow (1)$$

* $f(x)$ is cont at $x=4$

$$f(x) = \text{LHL} = \text{RHL}$$

$$2x+1 = \lim_{x \rightarrow 4^-} 7-qx = \lim_{x \rightarrow 4^+} 2x+1$$

$$2(4)+1 = 7-4q = 2(4)+1$$

$$8+1 = 7-4q = 9 \rightarrow (2)$$

From (2) $9 = 7-4q$

$$q = \frac{7-9}{4} = -\frac{2}{4}$$

Q. No. 3 (Page 2)

$$q = -\frac{1}{2}$$

from ①

$$7 - 2q = 2p + 2$$

$$7 - 2\left(-\frac{1}{2}\right) = 2p + 2$$

$$7 + 1 = 2p + 2 \Rightarrow 8 = 2p + 2$$

$$6 = 2p$$

$$p = 3$$

$$\begin{aligned} &7 - q(x) \\ &7 - \left(-\frac{1}{2}\right)x \end{aligned}$$

$$f(x) = \begin{cases} 3x + 2 & 0 \leq x < 2 \\ 7 + \frac{1}{2}x & 2 \leq x < 4 \\ 2x + 1 & 4 \leq x < 6 \end{cases}$$

x	0	1	1.99	2	3	3.99	4	5	5.99
$y = 3x + 2$	2	5	7.99	8					
$y = 7 + \frac{1}{2}x$				8	$17/2$ (8.5)	8.99	9		
$y = 2x + 1$							9	11	12.99

(graph - page 43)

Q. No. 4 (Page 1) tangent equation

$$\frac{x^2}{128} + \frac{y^2}{18} = 1 \rightarrow \textcircled{A} \quad 18x^2 + 128y^2 = 2304 \rightarrow \textcircled{B}$$

$$3x + 8y + 1 = 0$$

$$m = \text{slope} = -\frac{3}{8} \quad (\text{slope of tangent})$$

$$a^2 = 128$$

$$b^2 = 18$$

$$y = mx \pm \sqrt{a^2m^2 + b^2}$$

$$y = -\frac{3}{8}x \pm \sqrt{128\left(-\frac{3}{8}\right)^2 + 18}$$

$$= -\frac{3}{8}x \pm \sqrt{18 + 18}$$

$$y = -\frac{3}{8}x \pm 6 \quad (\text{Xply by 8})$$

$$8y = -3x \pm 48$$

$$\boxed{3x + 8y \pm 48 = 0} \rightarrow \textcircled{1}$$

Required tangents
of ellipse.

$$\text{from } \textcircled{1} \quad 3x + 8y \pm 48 = 0$$

$$\boxed{x = \frac{48 - 8y}{3}} \quad \text{put in}$$

Put in \textcircled{B}

$$18\left(\frac{48 - 8y}{3}\right)^2 + 128y^2 = 2304$$

$$\frac{218}{19} (2304 + 64y^2 - 768y) + 128y^2 = 2304$$

$$4608 + 128y^2 - 1536y + 128y^2 - 2304 = 0$$

$$256y^2 - 1536y + 2304 = 0$$

$$256(y^2 - 6y + 9) = 0$$

Q. No. 4 (Page 2)

$$y^2 - 6y + 9 = 0$$

$$y^2 - 3y - 3y + 9 = 0$$

$$y(y-3) - 3(y-3) = 0$$

$$(y-3)^2 = 0$$

$$\boxed{y = 3}$$

Put y in $\frac{48-8y}{3} = x$

$$\boxed{x = 8}$$

$(8, 3)$ is the point of contact.

Q. No. 4 (Page 3)

Lined writing area consisting of approximately 28 horizontal lines.

Q. No. 4 (Page 4)

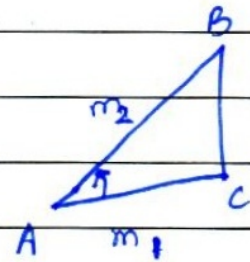
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Q. No. 5 (Page 1)

$$A (-3, -4) \quad (x_1, y_1)$$

$$B (4, 6) \quad (x_2, y_2)$$

$$C (4, -3) \quad (x_3, y_3)$$



Let m_1 and m_2 be the slopes of AB and AC.

$$\text{slope of AB} = m_2 = \frac{y_2 - y_1}{x_2 - x_1} = \frac{6 - (-4)}{4 - (-3)} = \frac{6 + 4}{4 + 3} = \frac{10}{7} \quad (m_2)$$

$$\text{slope of AC} = m_1 = \frac{-3 - (-4)}{4 - (-3)} = \frac{-3 + 4}{4 + 3} = \frac{1}{7} \quad (m_1)$$

(a)

i) Equation of AB side:

$$y - y_1 = m(x - x_1)$$

$$\therefore y - (-4) = \frac{10}{7}(x - (-3))$$

$$7(y + 4) = 10(x + 3)$$

$$7y + 28 = 10x + 30$$

$$\boxed{10x - 7y + 2 = 0}$$

ii) Equation of AC side:

$$y + 4 = \frac{1}{7}(x + 3)$$

$$7y + 28 = x + 3$$

$$\boxed{x - 7y - 25 = 0}$$

(b) $\angle A = ?$

$$\tan \theta = \frac{m_2 - m_1}{1 + m_1 m_2} = \frac{\frac{10}{7} - \frac{1}{7}}{1 + \left(\frac{10}{7}\right)\left(\frac{1}{7}\right)} = \frac{9/7}{59/49}$$

$$\tan \theta = \frac{63}{59}$$

$$\theta = \tan^{-1}(63/59)$$

$$A = \theta = 46.8 = 46^\circ 52'$$

$$\boxed{\angle A = 46.8^\circ}$$

c) Area of ΔABC :

$$\Delta = \frac{1}{2} \begin{vmatrix} -3 & -4 & 1 \\ 4 & 6 & 1 \\ 4 & -3 & 1 \end{vmatrix} \quad (\text{Expanding by } C_3)$$

$$= \frac{1}{2} [1(-12-24) - 1(9+16) + 1(-18+16)]$$

$$= \frac{1}{2} [-36 - 25 - 2]$$

$$= -63/2 \quad (\text{ignore -ve})$$

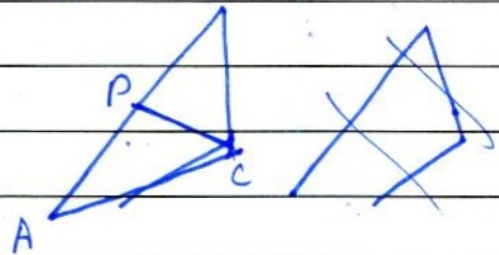
$$\Delta = 63/2 \text{ Sq. units.}$$

(d) Take Point P on AB ie CP is \perp to AB

$$\text{Slope of CP} = -\frac{1}{\text{Slope of AB}}$$

$$= -\frac{1}{10}$$

$$\text{Slope of CP} = -\frac{7}{10}$$



Let Point P(x, y) and C(4, -3)

Equation of line.

$$y + 3 = -\frac{7}{10}(x - 4)$$

$$10y + 30 = -7x + 28$$

$$7x + 10y + 2 = 0 \rightarrow \text{(A)}$$

$$10x - 7y + 2 = 0 \rightarrow \text{(B)}$$

Point of intersection of AB is P(x, y)

$$x = -4 = 1$$

$$\begin{vmatrix} 10 & 2 \\ -7 & 2 \end{vmatrix} \quad \begin{vmatrix} 7 & 2 \\ 10 & 2 \end{vmatrix} \quad \begin{vmatrix} 7 & 10 \\ 10 & -7 \end{vmatrix}$$

Q. No. 5 (Page 3)

$$\frac{x}{(20+14)} = \frac{-y}{(14-20)} = \frac{1}{(-49-100)}$$

$$\frac{x}{34} = \frac{-y}{-6} = \frac{1}{-149}$$

$$x = -\frac{34}{149}$$

$$y = -\frac{6}{149}$$

$$P(x, y) = \left(-\frac{34}{149}, -\frac{6}{149} \right) \quad C(4, -3)$$

distance CP (perpendicular distance)

$$|CP| = \sqrt{\left(4 + \frac{34}{149}\right)^2 + \left(-3 + \frac{6}{149}\right)^2}$$

$$= \sqrt{17.87 + 8.76}$$

$$= \sqrt{26.63}$$

$$|CP| = 5.16 \text{ units}$$

$$\text{or } \frac{63}{\sqrt{149}}$$

Q. No. 6 (Page 1)

$$9x^2 - y^2 - 12x - 2y + 2 = 0 \quad (\text{Add } -1 \text{ and } 4 \text{ to } b.)$$
$$(3x)^2 - 2(3x)(2) + 4 - (y^2 + 2(y) + 1) = -2 + 4 - 1$$
$$(3x - 4)^2 - (y + 1)^2 = 1$$

$$9x^2 - y^2 - 12x - 2y + 2 = 0$$
$$9\left(x^2 - \frac{12x}{9}\right) - 1(y^2 + 2(y) + 1) = -2 - 1$$

$$9\left(x^2 - \frac{4x}{3}\right) - (y + 1)^2 = -3$$

$$9\left(x^2 - 2(x)\left(\frac{2}{3}\right) + \left(\frac{2}{3}\right)^2\right) - (y + 1)^2 = -3 + \frac{18}{9}$$

$$9\left(x^2 - 2\left(\frac{2}{3}\right)x + \left(\frac{2}{3}\right)^2\right) - (y + 1)^2 = 3 \quad (\div \text{ by } 9)$$
$$\frac{(x^2 - 2\left(\frac{2}{3}\right)x + \left(\frac{2}{3}\right)^2)^2}{3/9} - \frac{(y + 1)^2}{3} = 1$$

$$\frac{(x^2 - \frac{4}{3}x + \frac{4}{9})^2}{1/3} - \frac{(y + 1)^2}{3} = 1$$

Centre

$$C = \left(\frac{2}{3}, -1\right)$$

as shifted parabola.

$$a^2 = \frac{1}{3} \Rightarrow a = \frac{1}{\sqrt{3}}$$

$$b^2 = 3$$

$$c^2 = 10/3 \Rightarrow c = \sqrt{\frac{10}{3}}$$

$$\text{Foci } (\pm c, 0) = \left(\frac{2 \pm \sqrt{10}}{3}, -1\right)$$

$$\text{Foci } = F\left(\frac{2 \pm \sqrt{30}}{3}, -1\right)$$

Q. No. 6 (Page 2)

$$\text{Vertices} = (\pm a, 0)$$

$$c = (2/3, -1)$$

$$= \left(\frac{2}{3} \pm \frac{1}{\sqrt{3}}, -1 \right)$$

$$\text{Vertices} = \left(\frac{2 \pm \sqrt{3}}{3}, -1 \right)$$

$$\text{Eccentricity } e = \frac{c}{a} = \frac{\sqrt{10}/\sqrt{3}}{1/\sqrt{3}}$$

$$e = \sqrt{10}$$

$$\text{Directrices } x = \pm \frac{a^2}{c}$$

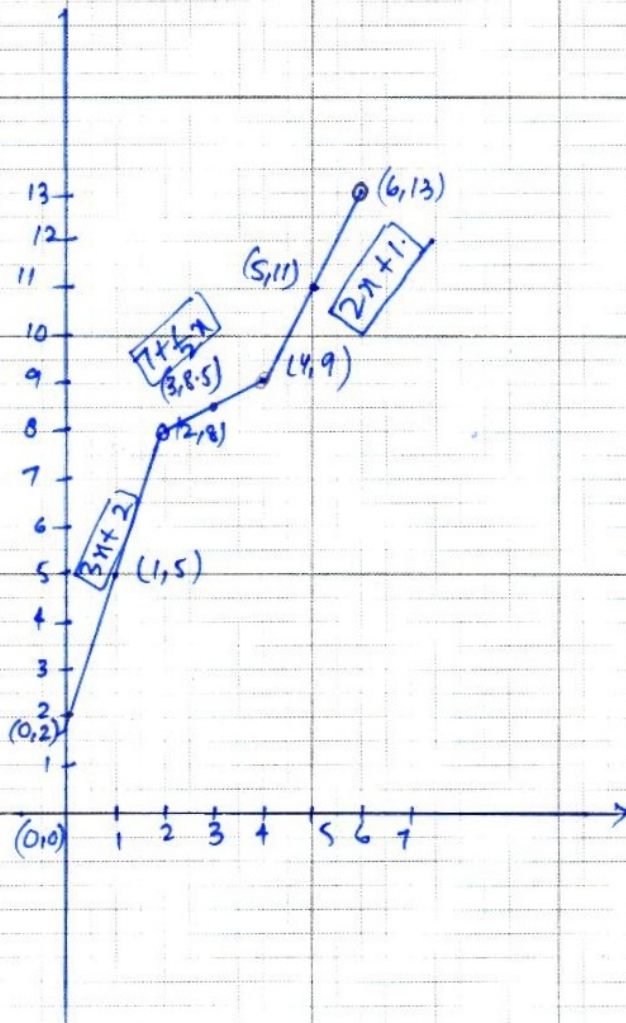
$$x - \frac{2}{3} = \pm \frac{1/3}{\sqrt{10/3}} = \pm \frac{1}{3} \div \frac{\sqrt{10}}{\sqrt{3}}$$

$$x - \frac{2}{3} = \pm \frac{1}{\sqrt{30}}$$

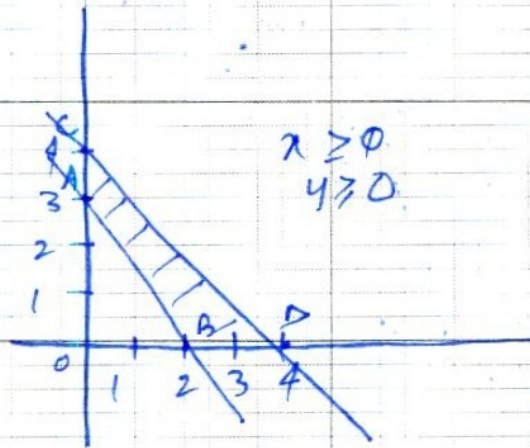
$$x = \frac{2}{3} \pm \frac{1}{\sqrt{30}}$$

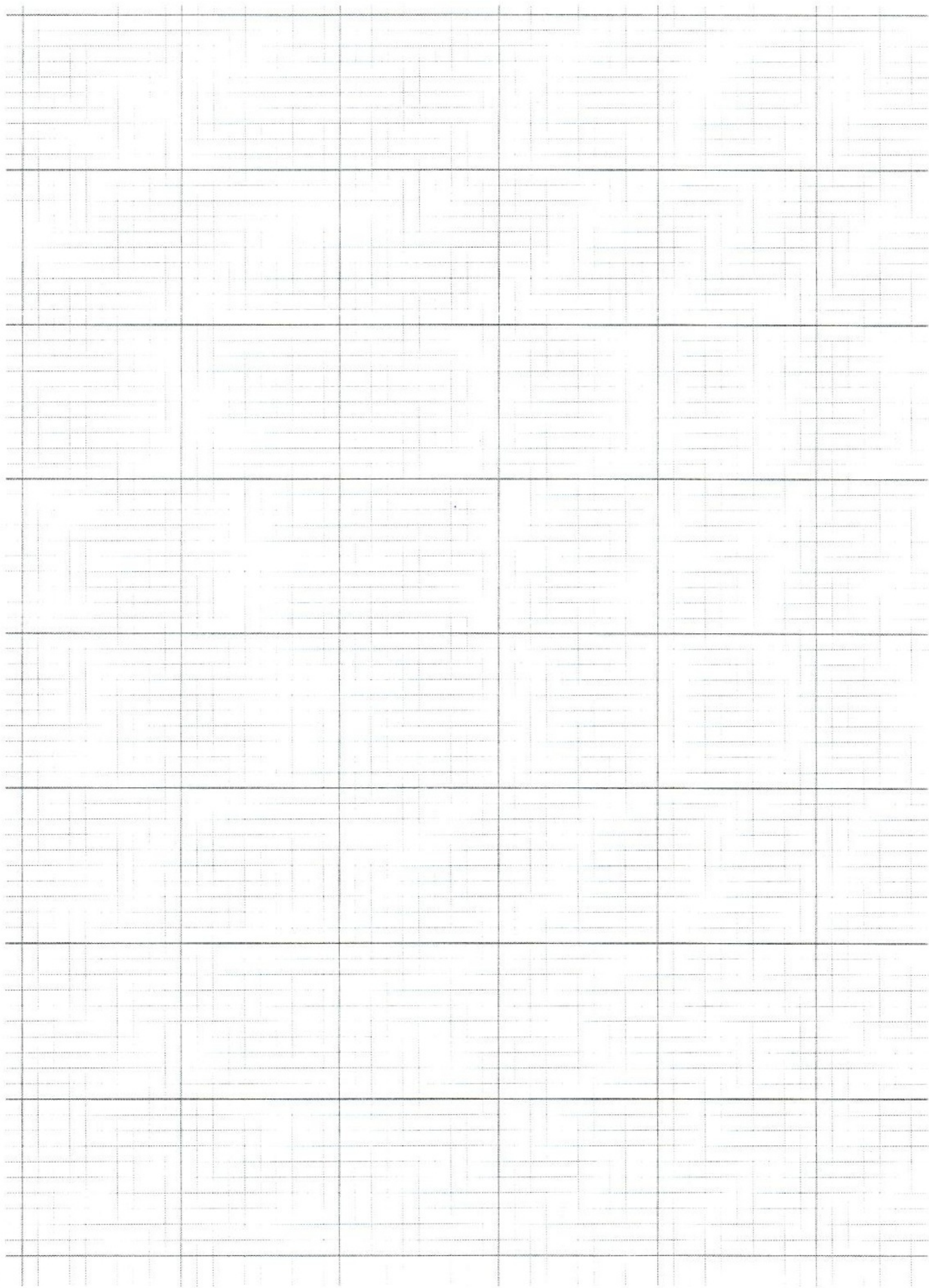
Q# 3
(Long)

Scale
 $x + y$ axis
2 small boxes = 1 unit.



2 small boxes
= 1 unit





$$v = x^2 y$$
$$\frac{dv}{dt} = 2xy \frac{dx}{dt} + x^2 \frac{dy}{dt}$$

$$x^2 + \frac{32}{x^2}$$

$$x^2 + \frac{32}{x^2}$$

$$f(x) = x^2 - 64x^{-3}$$



$$\sqrt{3} - \sqrt{3} + \sqrt{3}$$

$$\pi + 2$$

$$\pi + 2$$

$$\frac{\omega}{\epsilon}$$

2.1

$$x^2 + y^2 + 2x - 4y + \frac{1}{3} = 5 + \frac{1}{3} = \frac{16}{3}$$

$$L = 1 + 4 \cdot 4 \cdot \frac{1}{3}$$

$$1 + \frac{dy}{dx} = \cos(\pi + y) \left(1 + \frac{dy}{dx} \right)$$

$$= \cos(\pi + y) \frac{dy}{dx} + 1$$

$$-\frac{3}{k}$$

$$2x + 2$$

$$\frac{e}{\sin x}$$

$$-\int \frac{e^{\sin x}}{2}$$

$$-\frac{\sqrt{2}}{\pi} \left(\frac{1}{3} \right)$$

$$2 \left(-\frac{1}{2} \right)$$

$$\begin{pmatrix} x_1 & y_1 \\ 2 & 0 \\ x_2 & y_2 \\ 0 & -4 \end{pmatrix}$$

$$\frac{-4}{-2} \quad (2)$$

$$y - 0 = 2(x - 2)$$

$$y = 2x - 4$$

$$\begin{vmatrix} 3 & -1 & -2 \\ 5 & \alpha & -3 \\ 2 & 1 & -2 \end{vmatrix} = 0$$

$$2 \left(\frac{x^2}{2} - kx \right)$$

$$3(-2\alpha + 3) + 1(-10 + 6) - 2(5 - 2\alpha)$$

$$-6\alpha + 9 - 4 - 10 + 4\alpha = 0$$

$$-2\alpha \quad -5$$

$$2x + 2$$

$$x = \frac{1}{2}$$

$$-1 - 3$$

$$\frac{1}{4} - 4 = \frac{1}{4}$$

$$\sin^2 \left(e^{\sin x} \right)^2 = \frac{1}{2} \int e^t - 1$$